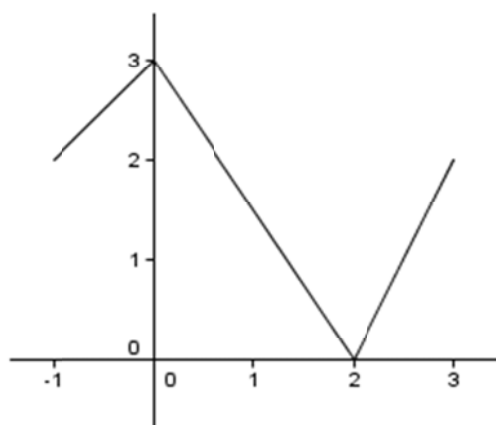


Practice Problems

1. Riemann sums. Sketch the region associated with the approximation, and then given the requested value.
- Give the upper sum for $f(x) = 4 - x^2$ on the interval $[-1, 1]$ with respect to the partition $P = \left\{-1, -\frac{1}{2}, \frac{1}{2}, 1\right\}$.
 - Give the lower sum for $f(x) = 4 - x^2$ on the interval $[-1, 1]$ with respect to the partition $P = \left\{-1, -\frac{1}{2}, \frac{1}{2}, 1\right\}$.
 - Give the midpoint approximation for $\int_{-1}^1 (4 - x^2) dx$ with respect to the partition $P = \left\{-1, -\frac{1}{2}, \frac{1}{2}, 1\right\}$.
 - Give the midpoint approximation for $\int_{-1}^1 (4 - x^2) dx$ using $n = 4$.
 - Give the left hand endpoint approximation for $\int_{-1}^1 (4 - x^2) dx$ using $n = 4$.
 - Give the right hand endpoint approximation for $\int_{-1}^1 (4 - x^2) dx$ using $n = 4$.
 - Use the graph of $f(x)$ below.



Give the upper sum for $f(x)$ on the interval $[-1, 3]$ with respect to the partition

$$P = \left\{-1, -\frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{5}{2}, 3\right\}.$$

2. Fundamental theorem of calculus.

a. $\frac{d}{dx} \int_{\pi}^x \sin(t) dt =$

b. $\frac{d}{dx} \int_{3x}^{\pi} \sin(t^2) dt =$

c. $\frac{d}{dx} \int_{3x}^{2x} \sin(t^2) dt =$

d. $\frac{d}{dx} \int_{1-2x}^{2x^3} \sin(t^2) dt =$

3. Basic Integration.

a. $\int_2^7 x\sqrt{x^2+2} dx =$

b. $\int (3\sec^2(r) - 2\sqrt{r-1}) dr =$

c. $\int_0^1 \frac{\cos(x)}{2+\sin(x)} dx =$

d. $\int_0^1 e^{-2x} dx =$

e. $\int_0^{\pi/4} \frac{2}{1+x^2} dx =$

f. $\int_0^{\pi/4} \sec(x) \tan(x) dx =$

g. $\int \frac{3t}{t^4+1} dt =$

4. Area. Graph each region and find the requested area.

a. Find the area bounded by the graph of $f(x) = 1 + x^2$ and the x -axis over the interval $[-1,1]$.

b. Find the area bounded by the graph of $f(x) = 1 - e^x$ and the x -axis over the interval $[0,1]$.

c. Find the area bounded by the graph of $f(x) = \sin(x)$ and the x -axis over the interval $[\pi/2, \pi]$.

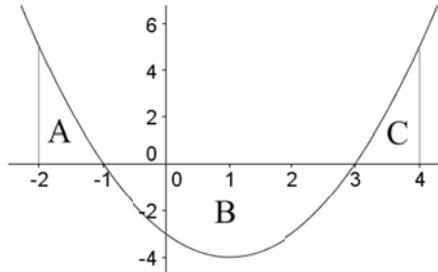
d. Give the area bounded between the x -axis and the graph of $f(x) = x^2 + 2x - 3$ over the interval $[-2,2]$.

5. Anti-derivatives.

- a. Give the general anti-derivative for $g(x) = x^3 + 2x - \sqrt{x}$.
- b. $F(x)$ is the anti-derivative for the function $x\sqrt{x^2 + 3}$ that satisfies $F(-1) = 2$. Give $3(F(0) - \sqrt{3}) + 1$.
- c. $F''(x) = x^2 - \frac{2}{\sqrt{x}} + 1$, $F'(1) = -3$ and $F(1) = 2$. Give $F(x)$.
- d. Find a formula for $f(x)$, given that $2x^3 - 3x^2 + x - 1 = \int_{-1}^x f(t) dt$.
- e. Suppose $f(x)$ is an anti-derivative of $r(x)$, and $g(x)$ is an anti-derivative of $s(x)$. We are given the data in the table about the functions f, g, r and s . $\int_1^3 (3r(x) - 2s(x)) dx =$

x	1	2	3	4
$f(x)$	3	2	1	4
$r(x)$	1	4	2	3
$g(x)$	2	1	4	3
$s(x)$	4	2	3	1

6. Use the following information in parts a-c. The graph of $f(x)$ is shown below, and $f(-2) = 5$. The area of region A is $7/3$, the area of region B is $34/3$, and the area of region C is $7/3$.



- Give the area of the region bounded between the graph of $f(x)$ and the x -axis on the interval $[-2, 4]$.
- $\int_{-1}^4 f(x) dx =$
- $\int_{-1}^{3/2} \left(3x - \frac{d}{dx} f(2x) \right) dx =$
- The graph of $y = g'(x)$ is shown below, and $g(1) = 1$. Give the values for $g(0)$, $g(2)$ and $g(3)$.

