## How Much Does a Grecian Urn?



A Grecian gentleman has the opportunity to urn a prize. He is given two urns and four marbles, two red and two white marbles. He may arrange the marbles in the two urns any way he chooses. Then another person will randomly draw one marble out of one of the urns. If the marble is white, the Grecian gentleman will urn the prize. If the marble is red, he will urn nothing.

The Grecian gentleman wants your help.

1. How could he best arrange the four marbles in the two urns to improve his chances of urning the prize?
2. Suppose he is required to put at least one marble in each of the urns. Will this affect how he should arrange the four marbles? Why or why not?
3. Repeat the problem, this time with 3 white and 2 red marbles.
4. Repeat the problem, this time with 2 white and 3 red marbles.
5. Repeat the problem, this time with 3 urns, 3 white and 3 red marbles.
6. Repeat the problem, this time with 3 urns, 2 white and 4 red marbles.
7. State and prove a conjecture concerning the arrangement that will maximize your chances of urning a prize.
