

# Car Trouble

**Purpose:**

Participants will use conditional probability to determine the chance of getting a good car repair job.

**Overview:**

In pairs, participants will use probability to determine aspects of their car repair given information about the productivity and quality of work done by the two mechanics in the auto repair shop.

**TEXES Mathematics 4-8 Competencies.** The beginning teacher:

- IV.013.B Uses the concepts and principles of probability to describe the outcome of simple and compound events.
- IV.013.C Generates, simulates, and uses probability models to represent a situation.
- IV.013.D Determines probabilities by constructing sample spaces to model situations.

**TEKS Mathematics Objectives.** The student is expected to:

- 4.13.A List all possible outcomes of a probability experiment such as tossing a coin.
- 4.13.B Use a pair of numbers to compare favorable outcomes to all possible outcomes.
- 5.12.A Use fractions to describe the results of an experiment.
- 6.9.A Construct sample spaces using lists, tree diagrams, and combinations.
- 6.9.B Find the probabilities of a simple event and its complement and describe the relationships between the two.
- 7.10.A Construct sample spaces for compound events (dependent and independent). ???
- 7.11.B Make inferences and convincing arguments based on an analysis of given or collected data.
- 8.11.A Find the probabilities of compound events (dependent and independent). ???
- 8.11.B Use theoretical probabilities and experimental results to make predictions and decisions.

**Terms.**

Conditional probability, sample space, complement of an event

**Materials.**

- Transparency
- Activity Sheet for each participant

**Transparencies.**

- *Car Trouble*
- *More Car Trouble*

**Activity Sheet(s).**

- *Car Trouble*
- *More Car Trouble*

**Procedure:**

<b>Steps</b>	<b>Questions/Math Notes</b>
<p>1. Read aloud the <i>Car Trouble</i> problem (Transparency) two times.</p> <p>Ask participants to work in pairs to answer the given questions about their auto repairs.</p>	<p>To stimulate their thinking, ask participants questions about what they are doing:</p> <p><i>What is the sample space for this problem? Is this a finite or infinite sample space? Explain.</i></p>
<p>2. Circulate among the groups as they work the problem.</p> <p>Ask participants to draw an area model or a tree diagram to represent the Car Trouble problem.</p>	<p><i>What are all the possible outcomes? How do you know?</i></p> <p><i>Which model (area model or tree diagram) will you choose to construct? Why?</i></p> <p><i>How many sections are needed for your area model?</i></p> <p><i>How many branches are needed for your tree diagram?</i></p> <p><i>Which questions include conditional statements and thus require the use of conditional probability?</i></p> <p><i>How are questions #3 and #4 (Activity Sheet) different? Explain.</i></p> <p><i>What is the condition in question #3?</i></p> <p><i>What is the condition in question #4?</i></p>
<p>3. Select several pairs to present their solution. Ask them to include an area model or a tree diagram that shows the possible outcomes.</p>	<p><i>Can you prove your answers are correct? Can you show another approach to obtain the same answers?</i></p> <p><i>Which model seems to better represent what is happening in the problem? Why?</i></p> <p><i>Which model assists you the most in answering the questions? Why?</i></p>

**Sample Space:** {(Axle, good job), (Axle, bad job), (Sparky, good job), (Sparky, bad job)}

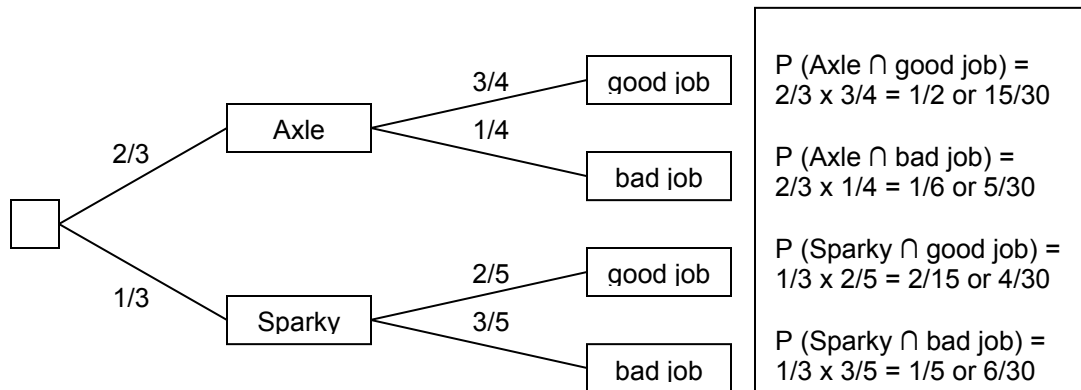
**Area Model:**

Axle 1/3	Axle 1/3	Sparky 1/3	
good job 1/12	good job 1/12	good job 1/15	$P(\text{Axle, good job}) = 1/2 \text{ or } 15/30$ $P(\text{Axle, bad job}) = 1/6 \text{ or } 5/30$ $P(\text{Sparky, good job}) = 2/15 \text{ or } 4/30$ $P(\text{Sparky, bad job}) = 1/5 \text{ or } 6/30$
good job 1/12	good job 1/12	good job 1/15	
good job 1/12	good job 1/12	bad job 1/15	
bad job 1/12	bad job 1/12	bad job 1/15	

**Area Model:**

Axle 2/3	Sparky 1/3	
$P(\text{Axle, good job}) =$ $2/3 \times 3/4 =$ $1/2$	$P(\text{Sparky, good job}) =$ $1/3 \times 2/5 =$ $2/15$	$P(\text{Axle, good job}) = 1/2 \text{ or } 15/30$ $P(\text{Axle, bad job}) = 1/6 \text{ or } 5/30$ $P(\text{Sparky, good job}) = 2/15 \text{ or } 4/30$ $P(\text{Sparky, bad job}) = 1/5 \text{ or } 6/30$
$P(\text{Axle, bad job}) =$ $2/3 \times 1/4 =$ $1/6$	$P(\text{Sparky, bad job}) =$ $1/3 \times 3/5 =$ $1/5$	

**Tree Diagram:**



**Solution:**

Use the formula for conditional probability which is  $P(A|B) = P(A \cap B) \div P(B)$

- $P(\text{good job}) = P(\text{Axle} \cap \text{good job}) + P(\text{Sparky} \cap \text{good job}) = 15/30 + 4/30 = 19/30$
- Use the formula for conditional probability which is  $P(A|B) = P(A \cap B) \div P(B)$   
 $P(\text{Sparky} | \text{good job}) = P(\text{Sparky} \cap \text{good job}) \div P(\text{good job}) = (4/30 \div 19/30) = 4/19$
- $P(\text{good job} | \text{Axle}) = P(\text{good job} \cap \text{Axle}) \div P(\text{Axle}) = 1/2 \div 2/3 = 3/4$   
(We didn't need to use the formula.  $P(\text{good job} | \text{Axle})$  is given information. Axle does a good job 3 out of 4 times.)

**Extension (additional questions):**

- What is the probability that a bad job will be done? ( $11/30$ )
- What is the probability that Axle worked on your car if a good job is done? ( $15/19$ )
- What is the probability that a bad job is done if Sparky worked on your car? ( $3/5$ )
- What is the probability that a good job is done if Sparky worked on your car? ( $2/5$ )
- What is the probability that Sparky worked on your car if a bad job is done? ( $6/11$ )
- What is the probability that Axle worked on your car if a good job is done? ( $15/19$ )